

An LR(0) item is a 2-tuple (a pair): (production, dot).

An LR(1) item is a 3-tuple: (production, dot, lookahead).

// I is a set of LR(1) items

```
fn lr1_closure(I) {  
  while changed {  
    for each item (P, d, a) in I {  
      if d == len(P) {  
        continue;  
      } else if P[d] is a terminal {  
        continue;  
      } else { // P[d] is a nonterminal {  
        for each production Q targeting P[d] {  
          for each terminal b in FIRST(P[d + 1:] + a) {  
            insert(I, (Q, 0, b));  
          }  
        }  
      }  
    }  
  }  
}
```

$P = A \rightarrow X Y Z X Y Z$   
 $d = 1$       ↑  
 $P[d] = Y$   
 $P[d+1:] = Z X Y Z$   
 $P[d+1:] + a = Z X Y Z a$

// I is a LR(1) set of items

// X is a symbol in our grammar

```
fn lr1_goto(I, X) {  
  result = {}  
  for (P, d, a) in I {  
    if d == len(P) {  
      continue;  
    } else if P[d] == X {  
      insert(result, (P, d + 1, a));  
    }  
  }  
}
```

// G is a grammar

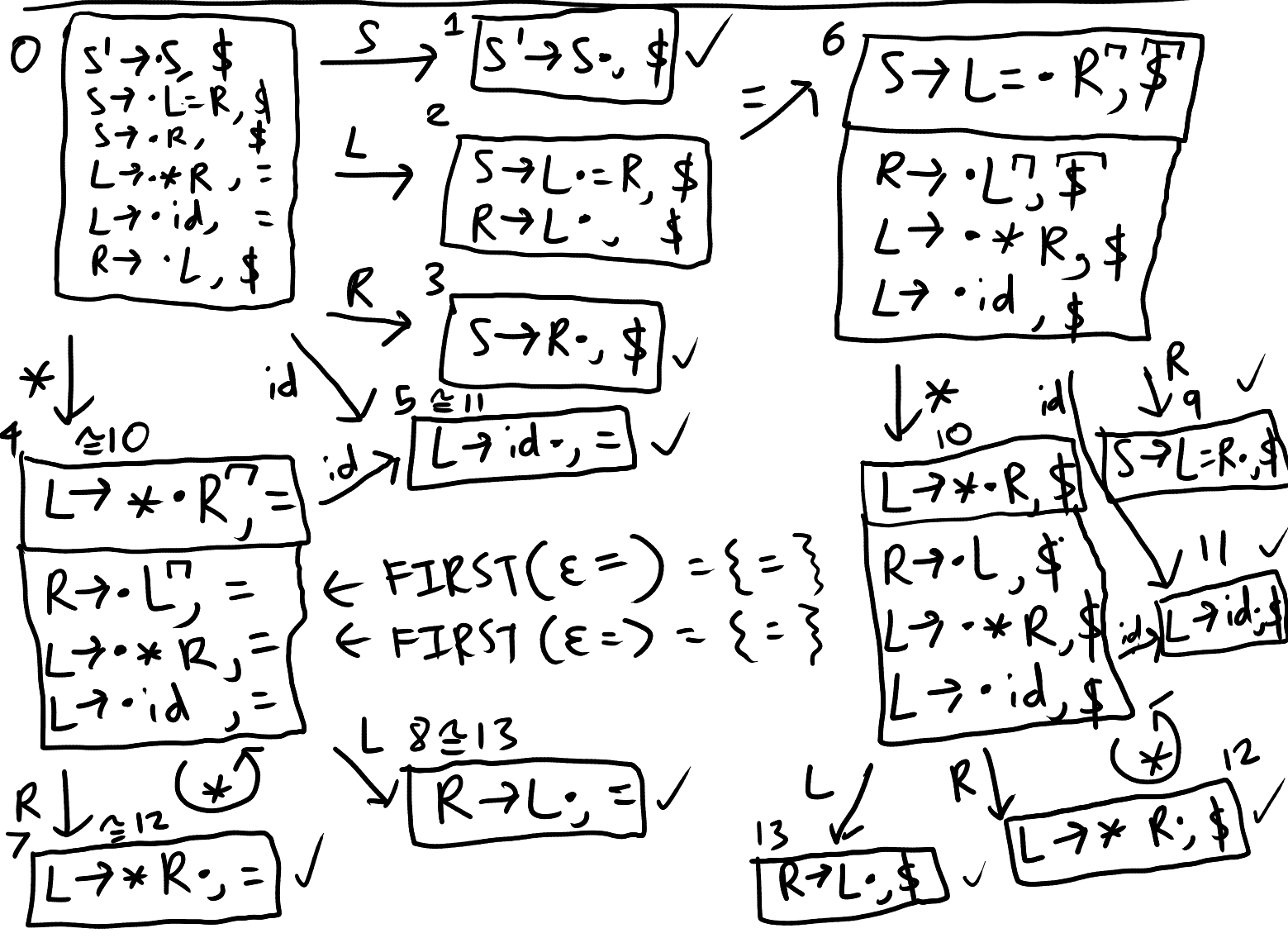
```
fn lr1_compute_states(G) {  
  start = closure({ (start' -> start, 0, $) });  
  states = { start };  
  while changed {  
    for state in states {  
      for symbol in G {  
        next_state = lr1_goto(state, symbol);  
        insert(states, next_state);  
      }  
    }  
  }  
}
```

①  $S' \rightarrow S$      $S \rightarrow L = R \mid R$      $L \rightarrow *R \mid id$      $R \rightarrow L$

$S' \rightarrow \cdot S, \$$   
 $S \rightarrow \cdot L = R, \$$   
 $S \rightarrow \cdot R, \$$   
 $L \rightarrow \cdot *R, =$   
 $L \rightarrow \cdot id, =$   
 $R \rightarrow \cdot L, \$$   
 ~~$R \rightarrow \cdot L, a$~~   
 ~~$R \rightarrow \cdot L, b$~~   
 ~~$R \rightarrow \cdot L, c$~~

$\leftarrow FIRST(\epsilon \$) = FIRST(\$) = \{\$ \}$   
 $\leftarrow FIRST(=R \$) = \{=\}$   
 $\leftarrow FIRST(\$) = \{\$, a, b, c\}$

$FIRST(S' \text{ or } S \text{ or } L \text{ or } R)$   
 $= *, id$   
 $FOLLOW(S' \text{ or } S) = \{\$ \}$   
 $FOLLOW(L \text{ or } R) = \{=, \$ \}$



# LALR(1)

$A \rightarrow a., c$   
 $B \rightarrow b., d$

$A \rightarrow a.; d$   
 $B \rightarrow b.; c$

the same # states  
 $LR(0) \not\subseteq SLR \not\subseteq LALR(1)$   
 $\not\subseteq LR(1)$

$A \rightarrow a., c/d$   
 $B \rightarrow b., c/d$

$\leftrightarrow$   $A \rightarrow a., c$   
 $A \rightarrow a., d$

$\leftrightarrow$   $B \rightarrow b., c$   
 $B \rightarrow b., d$

