

NULLABLE(terminal) = false

NULLABLE(sequence of symbols) = true iff none of the symbols are NOT NULLABLE

NULLABLE(production) = NULLABLE(RHS)

NULLABLE(nonterminal) = any of its productions are NULLABLE

FIRST(terminal) = { terminal }

FIRST( $X_1 X_2 \dots X_n$ ) = union of FIRST( $X_1$ ), FIRST( $X_2$ ), ..., FIRST( $X_k$ )  
where  $X_1, X_2, \dots, X_{k-1}$  are NULLABLE and  $X_k$  is NOT NULLABLE

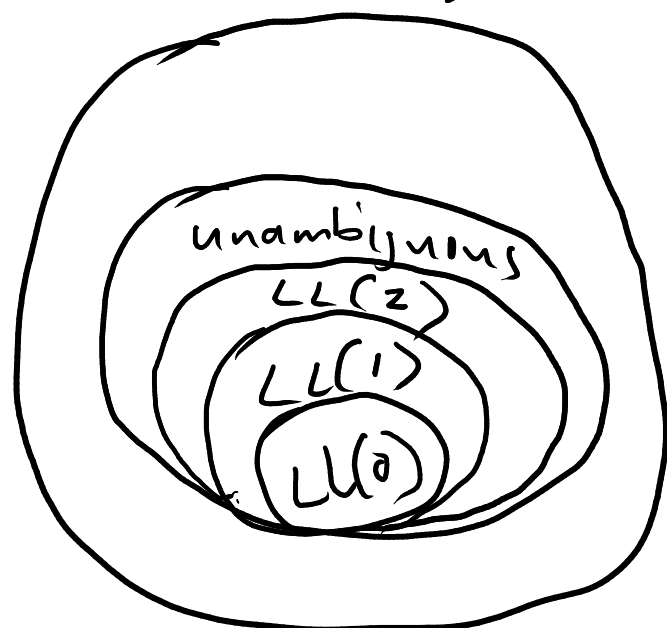
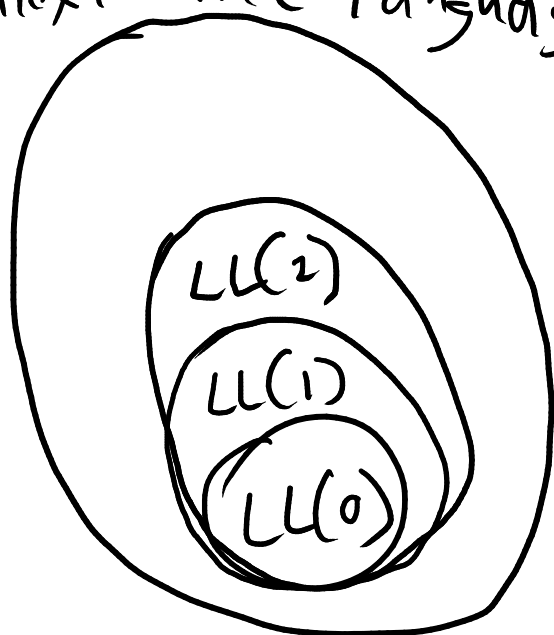
FIRST(production) = FIRST(RHS)

FIRST(nonterminal) = union of FIRST of RHS of its productions

grammar is LL(k) iff  
we can create an LL(k) parser

language is LL(k) iff

$\exists$  an LL(k) grammar for it  
context-free language      context-free grammars



Output is a 2d table  $M$

for each production  $P$  in the grammar {

$A = \text{lhs}(P)$

for each terminal  $a$  in  $\text{FIRST}(P)$  {

$M[A, a] = P$

if  $\text{NULLABLE}(P)$  { // equivalently, epsilon in  $\text{FIRST}(P)$

for each terminal  $b$  in  $\text{FOLLOW}(A)$  {

$M[A, b] = P$

1  $E \rightarrow TE'$

2  $E' \rightarrow +TE' \mid \text{epsilon}$

4  $T \rightarrow FT'$

5  $T' \rightarrow *FT' \mid \text{epsilon}$

7  $F \rightarrow (E) \mid \text{id}$

nonterminal

$E$

$E'$

$T$

$T'$

$F$

FIRST

(, id

+, epsilon

(, id

\*, epsilon

(, id

FOLLOW

), \$

), \$

+, ), \$

+, ), \$

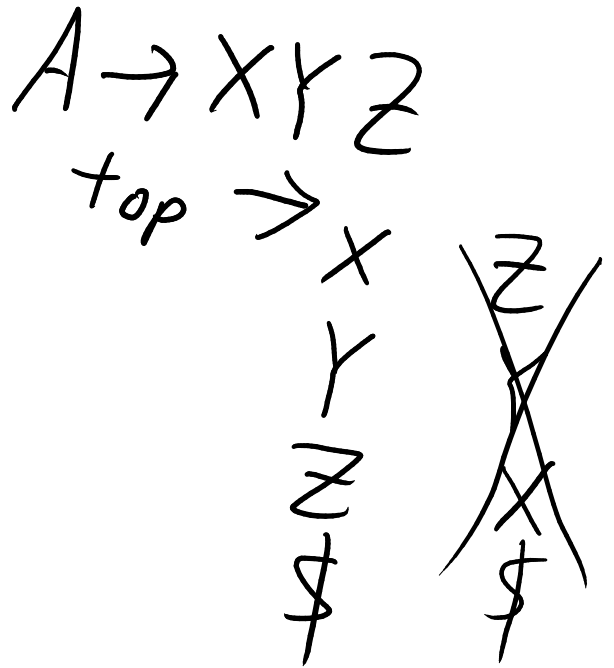
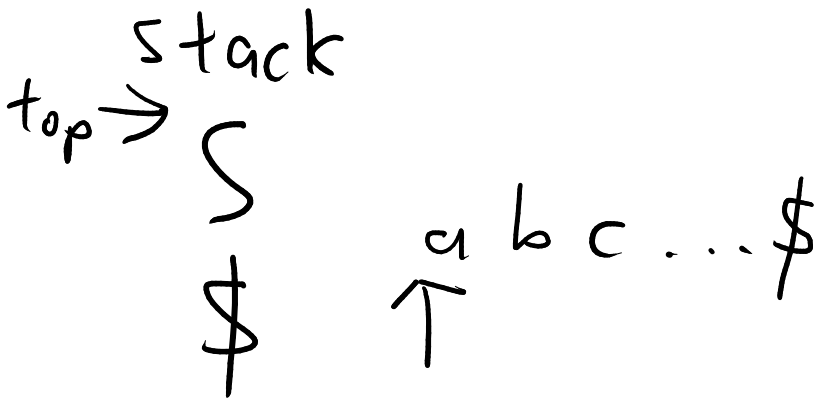
+, \*, ), \$

|      | ( | ) | + | * | id | \$ |
|------|---|---|---|---|----|----|
| $E$  | 1 |   |   |   | 1  |    |
| $E'$ |   | 3 | 2 |   |    | 3  |
| $T$  | 4 |   |   |   | 4  |    |
| $T'$ |   | 6 | 6 | 5 |    | 6  |
| $F$  | 7 |   |   |   | 8  |    |

```

// X refers to the top of the stack
// a refers to the next input token
while X != $ {
  if X is a terminal {
    if X == a {
      pop_stack();
      advance_input();
    } else {
      error();
    }
  }
  } else { // X is a nonterminal
    if M[X, a] is empty {
      error();
    } else {
      P = M[X, a];
      output(P);
      pop_stack();
      for Yi in reverse(rhs(P)) {
        push(Yi);
      }
    }
  }
}
return a == $;

```



if\_stmt → if ( expr ) {  
 statements  
 } else {  
 statements

