

# Optimal Scheduling Policy Determination in HSDPA Networks

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- 1 Objective and Motivation
- 2 Methodology
- 3 Problem Definition and Model Description
- 4 Case Study and Results
- 5 Conclusion and Future Work

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- Fair; Divide the resources fairly between all the active users.
- Optimal Transmission: Maximizes the overall cell throughput.
- Optimal Resource Utilization: Provide channel aware (diversity gain) and high speed resource allocation.

# Motivation

- 3GPP only suggested some guidelines for HSDPA downlink scheduler and left the design specifics undefined.
- This resulted in many different scheduling techniques and implementations most of which are proprietary.
- Most of the available work in scheduler design is based on intuition and creativity of the designers.

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- Study the structure of the optimal policy and develop a near-optimal heuristic policy.

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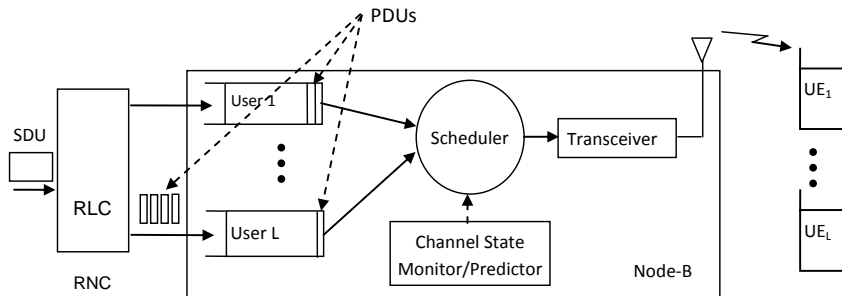
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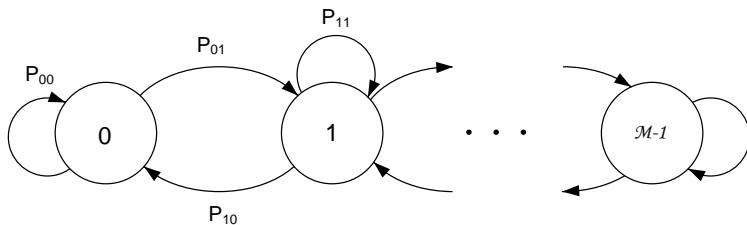
- Time is slotted into fixed length 2 ms **TTIs**.
- During each **TTI**, there are 15 available codes that may be allocated to one or more users.

# HSDPA Scheduler Model (Downlink)





# FSMC Model for HSDPA Downlink Channel



# The Model

- MDP based Model.
- HSDPA downlink scheduler is modelled by the 5-tuple  $(T, S, A, P_{ss'}(\mathbf{a}), R(\mathbf{s}, \mathbf{a}))$ ,  
where,
  - $T$  is the set of decision epochs,
  - $S$  and  $A$  are the state and action spaces,
  - $P_{ss'}(\mathbf{a}) = Pr(\mathbf{s}(t+1) = \mathbf{s}' | \mathbf{s}(t) = \mathbf{s}, \mathbf{a}(\mathbf{s}) = \mathbf{a})$  is the state transition probability, and
  - $R(\mathbf{s}, \mathbf{a})$  is the immediate reward when at state  $\mathbf{s}$  and taking action  $\mathbf{a}$ .

# Basic Assumptions

- $L$  active users in the cell.
- Finite buffer with size  $B$  per user for each of the  $L$  users.
- Error free transmission.
- SDUs are segmented by RLC into a fixed number of PDUs ( $u_i$ ) and delivered to Node-B at the beginning of the next TTI.
- Independent Bernoulli arrivals with parameter  $q_i$ .
- Scheduler can assign  $c$  codes chunks at a time, where  $c \in \{1, 3, 5, 15\}$  .

# Basic Assumptions—FSMC State Space

- The channel state of user  $i$  during slot  $t$  is denoted by  $\gamma_i(t)$ .
- Channel state space is the set  $\mathcal{M} = \{0, 1, \dots, M - 1\}$ .
- user  $i$  channel can handle up to  $\gamma_i(t)$  PDUs per code.

# State and Action Sets

- The system state  $\mathbf{s}(t) \in S$  is a vector and is given by

$$\mathbf{s}(t) = (x_1(t), x_2(t), \dots, x_L(t), \gamma_1(t), \gamma_2(t), \dots, \gamma_L(t)) \quad (1)$$

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- $a_i(t)c$ , number of codes allocated to user  $i$  at time epoch  $t$ .

# Reward Function

- The reward must achieve the **objective function**
- $R(\mathbf{s}, \mathbf{a})$  have two components corresponding to the two objectives

$$R(\mathbf{s}, \mathbf{a}) = \sum_{i=1}^L a_i \gamma_i c - \sigma \sum_{i=1}^L (x_i - \bar{x}) \mathbf{1}_{\{x_i=B\}} \quad (3)$$

where we defined the **fairness factor** ( $\sigma$ ) to reflect the significance of fairness in the optimal policy.

- The positive term of the reward maximizes the cell throughput.
- The second term guarantees some level of fairness and reduces dropping probability.

# State Transition Probability

- $P_{ss'}(\mathbf{a})$  denotes the probability that choosing an action  $\mathbf{a}$  at time  $t$  when in state  $\mathbf{s}$  will lead to state  $\mathbf{s}'$  at time  $t + 1$ .

$$\begin{aligned} P_{ss'}(\mathbf{a}) &= Pr(\mathbf{s}(t + 1) = \mathbf{s}' | \mathbf{s}(t) = \mathbf{s}, \mathbf{a}(t) = \mathbf{a}) \\ &= Pr(x'_1, \dots, x'_L, \gamma'_1, \dots, \gamma'_L | x_1, \dots, x_L, \gamma_1, \dots, \gamma_L, a_1, \dots, a_L) \end{aligned}$$

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- The evolution of the queue size ( $x_j$ ) is given by

$$\begin{aligned} x'_j &= \min([x_j - y_j]^+ + z'_j, B) \\ &= \min([x_j - a_j \gamma_j c]^+ + z'_j, B) \end{aligned} \tag{4}$$

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- Using the independence of the channel state and queue sizes

$$P_{ss'}(\mathbf{a}) = \prod_{i=1}^L \left( P_{x_i x'_i}(\gamma_i, a_i) P_{\gamma_i \gamma'_i} \right) \quad (5)$$

where  $P_{\gamma_i \gamma'_i}$  is the Markov transition probability of the **FSMC**.

## State Transition Probability cont.

$$P_{x_i x'_i}(\gamma_i, a_i) = \begin{cases} 1 & \text{if } x'_i = x_i = B \text{ \& } a_i \gamma_i = 0, \\ q_i & \text{if } x'_i = x_i = B \text{ \& } 0 < a_i \gamma_i c \leq u_i, \\ q_i & \text{if } x'_i = B \text{ \& } x_i < B \text{ \& } W1 \geq B, \\ q_i & \text{if } x'_i < B \text{ \& } x'_i = W1, \\ 1 - q_i & \text{if } x'_i < B \text{ \& } x'_i = W2, \\ 0 & \text{otherwise.} \end{cases} \quad (6)$$

where

$$W1 = [x_i - a_i \gamma_i c]^+ + u_i$$

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- The optimal policy is characterized by

$$V^*(\mathbf{s}) = \max_{\mathbf{a} \in A} [R(\mathbf{s}, \mathbf{a}) + \lambda \sum_{\mathbf{s}' \in S} P_{\mathbf{ss}'}(\mathbf{a}) V^*(\mathbf{s}')] \quad (7)$$

where,  $V^*(\mathbf{s}) = \sup_{\pi} V^\pi(\mathbf{s})$ , attained when applying the optimal policy  $\pi^*$ .

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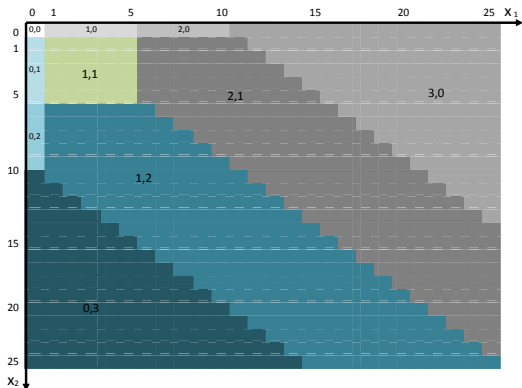
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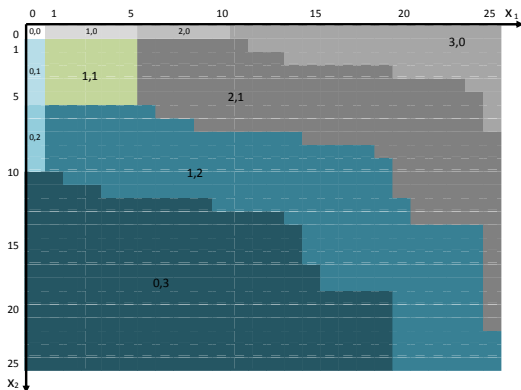
- The model was solved numerically using **Value Iteration**.

# The Optimal Policy for Two Symmetrical Users



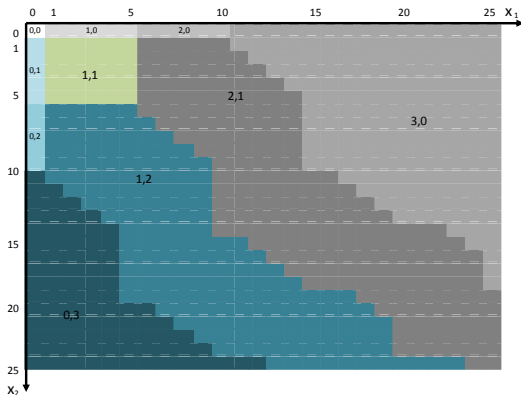
$P(\gamma_i = 1) = 0.5$  and  $P(z_i = 5) = 0.5$  for all  $i \in \{1, 2\}$ ;  $c = 5$ .

# The Effect of Channel Quality on Policy Structure



$$P(\gamma_1 = 1) = 0.8, \quad P(\gamma_2 = 1) = 0.5 \quad \text{and} \quad P(z_i = 5) = 0.5.$$

# The Effect of Arrival Probability on Policy Structure



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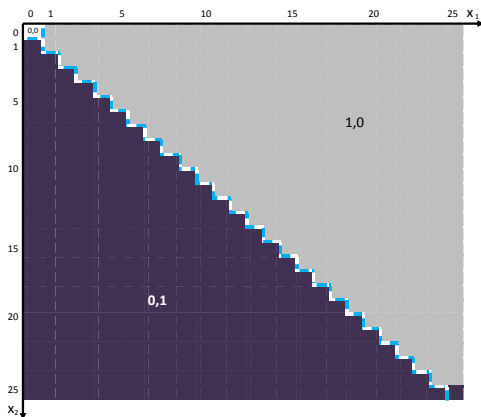
# Weight Function Approximation

Following these observations, we approximated  $w_1$  and  $w_2$  as follows

$$\hat{w}_1 = 1 + 1.5[-\Delta P_\gamma]^+ - 0.7[-\Delta P_z]^+ \quad (10)$$

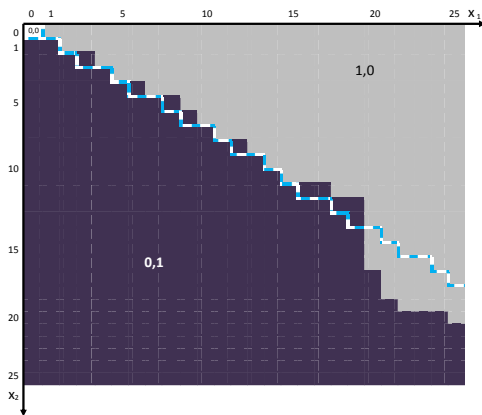
$$\hat{w}_2 = 1 + 1.5[\Delta P_\gamma]^+ - 0.7[\Delta P_z]^+ \quad (11)$$

# Heuristic (dotted line) vs. optimal policy; $c = 15$



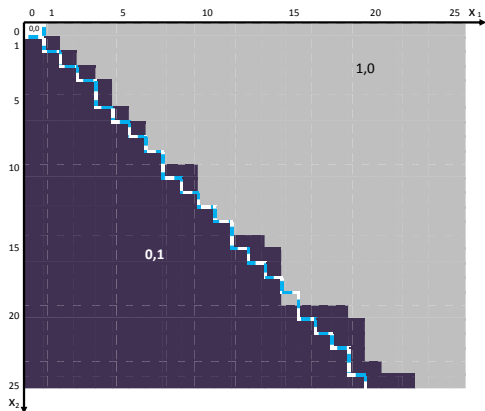
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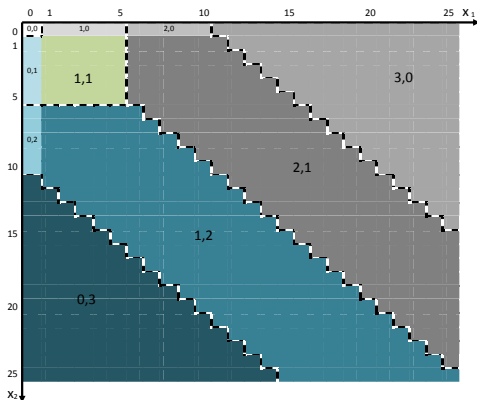
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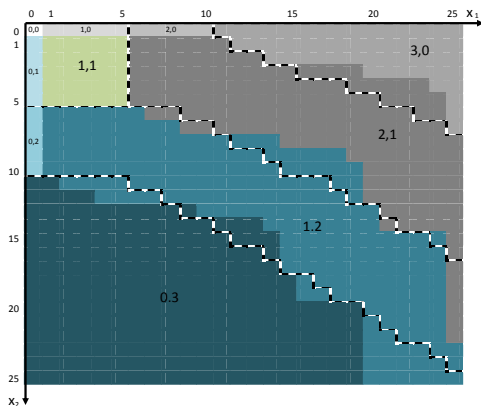
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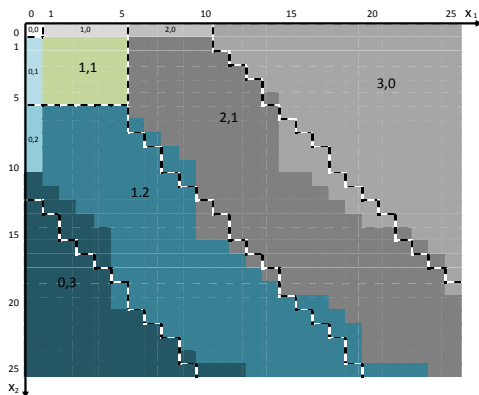


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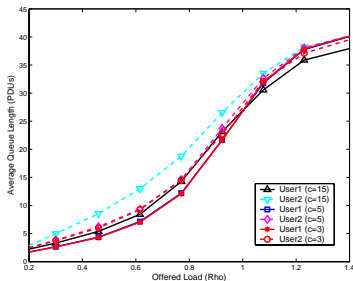
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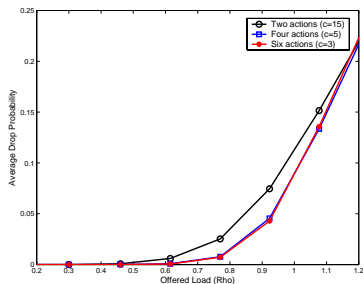


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# Performance Evaluation: The Effect of Policy Granularity



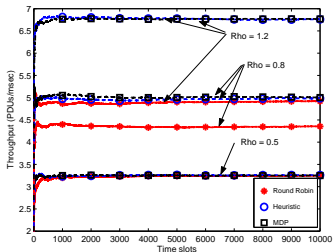
(a) on Average Queue Length



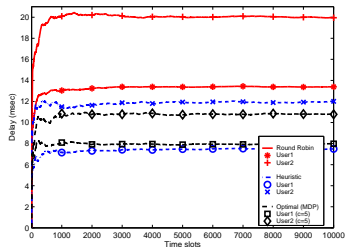
(b) on Average Drop Probability

Where  $\rho = \sum_i P_{z_i} u_i / r^\pi$  is the offered load and  $r^\pi$  is the measured system capacity under  $\pi$ .  $P(\gamma_1 = 1) = 0.8$  and  $P(\gamma_2 = 1) = 0.5$ .

# Heuristic Policy Evaluation



(c) System Throughput for different  $\rho$ ;  $P(\gamma_1 = 1) = 0.8$  and  $P(\gamma_2 = 1) = 0.5$ .



(d) Queueing Delay Performance;  $P(\gamma_2 = 1) = 0.5$ ,  $q_1 = 0.8$ ,  $q_2 = 0.5$  and  $u = 10$ .

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- A policy with finer granularity will perform better in light to moderate loading conditions, while a coarse policy is more desirable in heavy loading conditions.
- However, the performance gain when using  $c < 5$  is marginal and does not justify the added complexity.

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- The performance of the resulted heuristic policy matches very closely to the optimal policy.
- The results also proved that RR is undesirable in HSDPA system due to the poor performance and lack of fairness.
- The suggested heuristic policy can be extended to the case with more than two active users. It also can be easily adapted to accommodate more than one class of service.

# Future Work

- Prove analytically some of the optimal policy and value function characteristics, such as monotonicity, multi-modularity, and the switch-over behavior that we noticed before.

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- Relax the assumption of error free transmission and extend the model to take into account retransmissions.
- Study the effect of using different arrival process statistics using simulation obviously.

# Thank You

Discussion

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# Acronyms

- HSDPA–High Speed Downlink Packet Access.
- 3GPP–Third Generation Partnership Project
- MDP–Markov Decision Process
- TDMA–Time Division Multiple Access
- CDMA–Code Division Multiple Access
- TTI–Transmission Time Interval (2 ms)
- FSMC–Finite State Markov Channel
- SDU–Service Data Unit
- RLC–Radio Link Control Protocol located at Radio Network Controller (RNC)
- PDU–Protocol data unit
- LQF–Longest Queue First